



Review Article

Application of Scheffe's Simplex Lattice Model in concrete mixture design and performance enhancement

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ARTICLE INFO

Article history

Received: 17 December 2023

Revised: 01 March 2024

Accepted: 07 March 2024

Key words:

Concrete mix optimization;
Scheffe's Simplex Lattice Model;
Statistical methods; Material
properties; Sustainability

ABSTRACT

This comprehensive literature review delves into the application of Scheffe's Simplex Lattice Model for optimizing cement concrete mixtures, with a particular emphasis on its impact on material properties and sustainability. The review meticulously outlines the principles, historical context, and advantages of Scheffe's model, providing a nuanced understanding of its significance. Comparative analyses with traditional and alternative optimization techniques in concrete mix design illuminate the distinct advantages of statistical methods, especially Scheffe's model. The review critically examines the challenges and limitations associated with applying Scheffe's model, addressing issues related to the complexity of concrete mixtures and computational demands. Potential avenues for improvement are explored, suggesting refinements to handle non-linearity, incorporate advanced optimization algorithms, and streamline computational requirements. Additionally, the review highlights emerging trends in statistical modeling for concrete mixture optimization, such as the integration of machine learning and data-driven approaches, signaling the evolving landscape of concrete technology. In conclusion, the literature underscores Scheffe's Simplex Lattice Model as a valuable and versatile tool with far-reaching implications for the advancement of concrete mixture design methodologies. The call to action encourages ongoing research and development to refine the model, explore emerging trends, and address practical challenges, positioning Scheffe's model as a cornerstone in the pursuit of sustainable, resilient, and high-performance concrete materials.

Cite this article as: Agunwamba J, Okafor F, Tiza MT. Application of Scheffe's Simplex Lattice Model in concrete mixture design and performance enhancement. Environ Res Tec 2024;7(X)00–00.

INTRODUCTION

The optimization of concrete mixtures is crucial for ensuring the strength, durability, and overall performance of structures, especially in the face of growing demands for enhanced material properties and sustainability. The complex nature of concrete mixtures, influenced by numerous variables, poses a challenge in achieving an ideal balance. This literature review focuses on statistical methods in concrete mixture optimization, particularly Scheffe's Simplex Lattice Model, recognized for efficiently exploring and optimizing

multi-variable systems. By unraveling the model's principles and examining its applications, the review aims to contribute insights into its potential to revolutionize concrete mixture design. It comprehensively surveys existing studies, evaluating methodologies and outcomes, with the overarching goal of advancing concrete technology and providing valuable guidance to researchers and practitioners in the field. The scope encompasses a diverse range of studies, methodologies, and outcomes related to Scheffe's model, offering a holistic perspective on its successes, challenges, and future potential in shaping the future of concrete mixture design.

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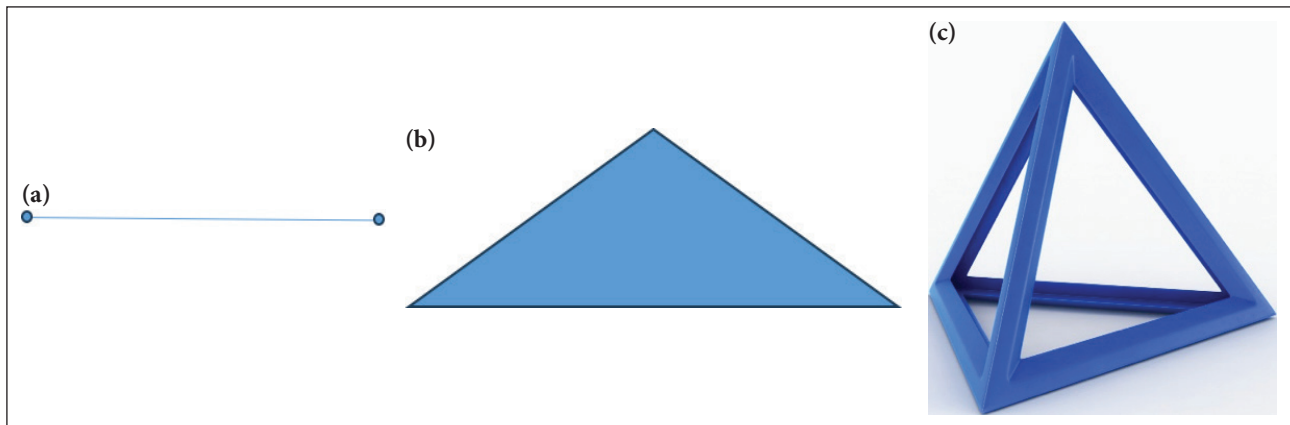


Figure 1. (a) Scheffe's simplex lattice design, when q is 2. (b) Scheffe's simplex lattice when q is 3. (c) Scheffe's simplex lattice design, when q is 4 (Tetrahedron Shape).

SCHEFFE'S SIMPLEX LATTICE MODEL OVERVIEW AND PRINCIPLES

Explanation of Scheffe's Simplex Lattice Model

Scheffe's Simplex Lattice Model is a statistical tool designed for optimizing complex systems with multiple variables. Developed by statistician Henry Scheffe (1958), this model is particularly suited for mixture design, enabling researchers and engineers to navigate intricate parameter spaces efficiently. At its core, the model employs a simplex, a geometric shape formed by connecting points in multi-dimensional space, to iteratively explore and converge towards optimal combinations of variables [1]. By systematically probing the experimental space, Scheffe's Simplex Lattice Model facilitates the identification of optimal concrete mixtures. The process begins by defining parameters $\{q, n\}$ for the Simplex Lattice Model, generating a design with uniformly spaced points for each component.

In a mixture experiment with q components, think of a lattice as a well-ordered pattern of points. For Scheffe's simplex lattice design, when q is 2, it is like 2 points forming a straight line as depicted in Figure 1a. When q is 3, it resembles an equilateral triangle as depicted in Figure 1b, and for q equal to 4, it takes the shape of a regular tetrahedron as depicted in Figure 1c.

Scheffe's idea suggests that each component in the mixture design sits on a corner (vertex) of this lattice, with a factor space of $(q-1)$. If we denote the degree of the polynomial as ' n ,' a $\{q, n\}$ simplex lattice for q components has evenly spaced points created by all possible combinations of $(n+1)$ levels for each component.

Concrete properties, according to Scheffe, depend on the right proportioning of its components, not the total mass. So, Scheffe's optimization theory, using polynomial regression, helps model and optimize concrete properties.

Actual ratios are determined through experience, and pseudo ratios are calculated [2]. Experiments are conducted to obtain response values, and model equations are fitted using the Least Squares Method. The model is validated, and

mix proportions are optimized, with experiments verifying predictions. Results are analyzed, and the process concludes [3–5]. Refer to Figure 2 for the visual representation of this comprehensive flowchart.

Historical Context and Development of the Model

The historical evolution of Scheffe's Simplex Lattice Model traces back to the mid-20th century when Henry Scheffe introduced it as a powerful statistical tool [6]. Stemming from advancements in experimental design and statistical analysis, the model emerged as a response to the increasing complexity of industrial processes, including the intricate nature of concrete mixture optimization. Its development represents a pivotal moment in statistical modeling, demonstrating a tailored approach for efficiently exploring and optimizing intricate parameter spaces [7].

Basic Principles and Mathematical Foundations

The model's fundamental principles rest on the simplex method, a mathematical optimization technique used to navigate complex spaces [8]. The simplex is a geometric shape with vertices representing different combinations of variables [9]. Scheffe's model employs a systematic process of moving toward optimal combinations by iteratively adjusting the vertices. Mathematically, this involves solving linear programming problems, minimizing or maximizing an objective function subject to certain constraints [10]. The model's elegance lies in its ability to efficiently converge towards optimal solutions, even in high-dimensional spaces [10, 11].

Advantages and Unique Features of Scheffe's Simplex Lattice Model in the Context of Concrete Mixture Optimization

Scheffe's Simplex Lattice Model offers distinct advantages in the realm of concrete mixture optimization. Its systematic approach allows for the exploration of a wide range of variables simultaneously, enabling researchers to identify optimal combinations efficiently [12]. The model's adaptability to high-dimensional spaces is particularly beneficial in the intricate context of concrete mixtures, where

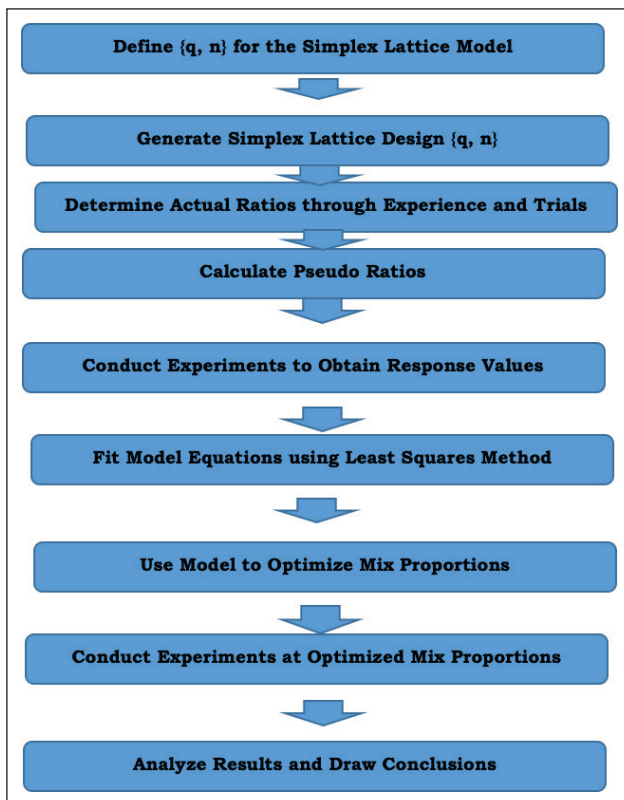


Figure 2. Visual representation of optimization process using Scheffe's Simplex Lattice Model in concrete mix design.

multiple components interact to determine the material's properties [13]. Additionally, Scheffe's model provides a structured methodology for researchers to understand and refine the relationships between variables, offering valuable insights into the optimization process. Its application in concrete mixture design demonstrates a unique ability to balance variables effectively, resulting in improved material performance and durability [14]. Table 1 summarizes the key advantages of Scheffe's Simplex Lattice Model in concrete mixture optimization.

HISTORICAL DEVELOPMENT OF MIXTURE DESIGN TECHNIQUES IN CONCRETE

Evolution of Concrete Mixture Design Methodologies

The evolution of concrete mixture design methodologies reflects a progression from empirical methods to more systematic and scientific approaches [15]. Initially, concrete mixtures were formulated based on experience and rules of thumb. Over time, advancements in material science, engineering, and statistical methods have driven the development of more sophisticated and precise mixture design techniques [16]. The evolution represents a shift towards a more comprehensive understanding of the complex interactions among various components in concrete [16]. As depicted in Figure 3, this flowchart visually represents the evolution of concrete mixture design methodologies. The progression begins with empirical methods rooted in experience and rule of thumb formulations, transitioning

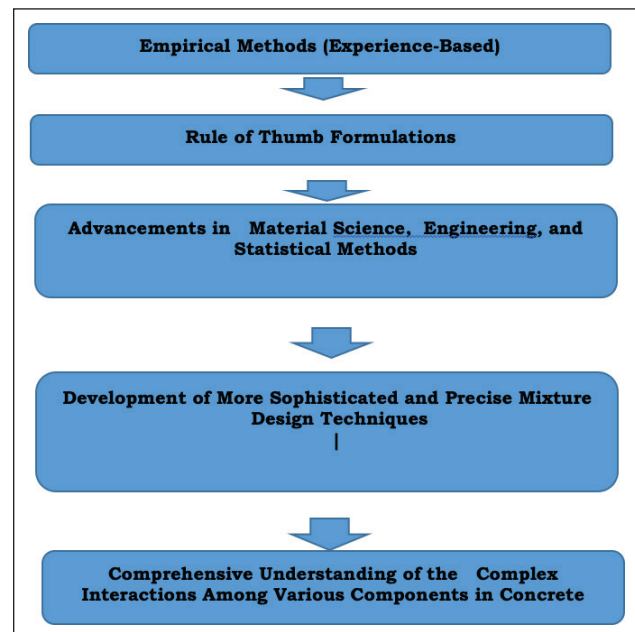


Figure 3. Flowchart visually representing the evolution of concrete mixture design methodologies.

towards more sophisticated and precise techniques driven by advancements in material science, engineering, and statistical methods.

Key Milestones and Advancements Leading to the Adoption of Statistical Methods

Key milestones in concrete mixture design include the recognition of statistical methods as powerful tools for optimizing material properties [17]. As the demand for high-performance concrete increased, researchers sought more rigorous and efficient approaches. The adoption of statistical methods gained momentum with the realization that they could systematically explore the vast design space of concrete mixtures [18]. Milestones include the integration of factorial experiments and response surface methodologies, paving the way for the utilization of advanced statistical models like Scheffe's Simplex Lattice Model [19].

Comparison with Other Optimization Techniques Used in Concrete Mix Design

Comparing statistical methods, such as Scheffe's Simplex Lattice Model, with other optimization techniques in concrete mix design reveals distinct advantages. Traditional methods often rely on trial-and-error approaches, whereas statistical models provide a systematic and data-driven framework for optimization [20]. Statistical methods can efficiently handle multiple variables simultaneously, offering a holistic approach to mixture design. In contrast, deterministic methods may struggle to navigate complex parameter spaces. Moreover, statistical models, by considering interactions between variables, contribute to a more nuanced understanding of the concrete mixture, leading to improved performance and durability compared to some traditional optimization techniques [21].

Table 1. Advantages of Scheffe's Simplex Lattice Model in concrete mixture optimization

Aspect	Description	Reference
Systematic approach	Simultaneous exploration of multiple variables for efficient identification of optimal combinations[12].	[12]
Adaptability to high-dimensional spaces	Crucial in the complex context of concrete mixtures, excelling in navigating intricate, multi-variable systems[13].	[13]
Structured methodology	Provides a systematic framework for understanding and refining relationships between variables in optimization processes[14].	[14]
Effective balancing of variables	Uniquely balances variables, contributing to improved material performance and durability in concrete mixture design[14].	[14]

Table 2. Comparative analysis of statistical methods in concrete mix design

Aspect	Comparison	Reference
Approach	Statistical methods (e.g., Scheffe's Simplex Lattice Model) provide a systematic, data-driven alternative to traditional trial-and-error approaches.	[20]
Handling multiple variables	Statistical methods efficiently manage multiple variables, offering a holistic approach, while deterministic methods may struggle in complex spaces.	[20]
Consideration of interactions	Models like Scheffe's consider interactions, contributing to nuanced understanding and improved performance.	[21]
Evolutionary milestones	Evolution highlights a shift from empirical to statistically driven approaches for precision and efficiency.	[22]
Advantages in design spaces exploration	Statistical models systematically explore complex design spaces, uncovering nuanced relationships, enhancing concrete mix design.	[23]

In summary, the evolution of concrete mixture design methodologies has witnessed a transition from empirical practices to sophisticated, statistically driven approaches. Key milestones underscore the importance of adopting statistical methods for precision and efficiency [22]. When compared with other optimization techniques, statistical models stand out for their systematic exploration of complex design spaces and their ability to uncover nuanced relationships between variables, making them valuable tools in advancing the field of concrete mix design [23]. Table 2 provides a concise comparison of statistical methods, particularly Scheffe's Simplex Lattice Model, with other optimization techniques in concrete mix design, along with relevant references.

METHODOLOGICAL APPLICATIONS IN CEMENT CONCRETE STUDIES

Review of Studies Applying Scheffe's Simplex Lattice Model in Optimizing Concrete Mixtures

Numerous studies have leveraged Scheffe's Simplex Lattice Model to optimize concrete mixtures, showcasing its versatility and effectiveness in enhancing material properties [24]. These investigations span a range of applications, from achieving specific strength requirements to improving durability and sustainability. The review highlights the methodologies employed in these studies, emphasizing the diversity of concrete mixtures addressed and the outcomes achieved through the application of Scheffe's model.

Description of Variables Considered in These Studies

In the studies employing Scheffe's Simplex Lattice Model, a variety of critical variables are systematically considered to optimize concrete mixtures. These variables often include the water-cement ratio, a crucial factor influencing both the workability and strength of concrete [24]. Aggregate types, encompassing size, gradation, and source, are meticulously examined for their impact on mechanical and durability properties [25]. Additionally, the incorporation of admixtures, such as superplasticizers or pozzolans, adds another layer of complexity to the optimization process. The literature review details how these studies strategically manipulate and assess these variables within the context of Scheffe's model to achieve desired concrete performance [26].

Discussion on How the Model Accounts for Interactions Between Different Components in the Concrete Mix

Scheffe's Simplex Lattice Model excels in its ability to account for the intricate interactions between different components in a concrete mix [27]. The model operates by systematically varying the levels of each variable, observing the resulting changes in the mixture's properties. Through this iterative process, Scheffe's model captures not only the individual effects of variables but also their interactions [28]. For instance, it assesses how the water-cement ratio influences the performance of specific aggregate types or how the addition of an admixture interacts with varying proportions of cementitious materials [29]. By comprehensively exploring these interdependencies, the model provides valuable insights into the nuanced relationships among

Table 3. Interactions among concrete Mix Components Using Scheffe's Model

Interaction type	Description	Reference
Water-cement ratio vs. aggregate types	Scheffe's model systematically analyzes how variations in the water-cement ratio influence the performance of specific aggregate types.	[29]
Admixture impact on cementitious materials	The model explores interactions, revealing how the addition of an admixture interacts with varying proportions of cementitious materials.	[29]

Table 4. Performance evaluation of concrete mixtures optimized with Scheffe's Simplex Lattice Model

Performance indicator	Description	Reference
Compressive strength	Assessment of the concrete's ability to withstand loads, a key metric reflecting its structural integrity.	[34]
Durability	Evaluation includes resistance to abrasion, freeze-thaw cycles, and chemical exposure, indicating long-term sustainability.	[34]
Workability	Analysis of the concrete's ease of placement and compaction, contributing to practical application.	[35]
Setting time	Examination of the time taken for the concrete to set, influencing construction timelines.	[35]
Shrinkage	Assessment of the concrete's tendency to shrink during curing, a critical consideration for structural integrity.	[35]

different components, guiding the optimization process towards achieving the desired concrete mixture characteristics [30]. In essence, the studies reviewed demonstrate the efficacy of Scheffe's Simplex Lattice Model in optimizing concrete mixtures by considering and manipulating key variables. The nuanced exploration of interactions between different components, facilitated by the model, contributes to a more profound understanding of the intricate relationships within concrete mixes, ultimately leading to improved and tailored material performance [31]. Table 3 succinctly outlines the ways Scheffe's Simplex Lattice Model addresses and understands the intricate interactions among different components in concrete mixes.

PERFORMANCE EVALUATION OF OPTIMIZED CONCRETE MIXTURES

Evaluation of Concrete Mixtures Optimized Using Scheffe's Simplex Lattice Model

The evaluation of concrete mixtures optimized through Scheffe's Simplex Lattice Model reveals the model's impact on enhancing material properties [32]. This process involves a systematic assessment of the optimized mixtures in real-world conditions. Researchers and practitioners critically examine the performance of the concrete to determine the effectiveness of the Scheffe's model in achieving desired outcomes [33].

Analysis of Performance Indicators

Concrete mixtures optimized using Scheffe's Simplex Lattice Model undergo a thorough analysis of various performance indicators. These indicators encompass fundamental properties such as compressive strength, a key metric reflecting the concrete's ability to withstand loads

[34]. Durability assessments, including resistance to abrasion, freeze-thaw cycles, and chemical exposure, provide insights into the long-term sustainability of the optimized mixtures. Other relevant properties, such as workability, setting time, and shrinkage, contribute to a comprehensive understanding of the concrete's overall performance [35]. The analysis delves into how Scheffe's model influences these indicators, showcasing the model's effectiveness in tailoring concrete mixtures to meet specific performance criteria. Table 4 concisely summarizes the performance evaluation of concrete mixtures optimized through Scheffe's Simplex Lattice Model, covering key indicators and their references.

Comparison with Traditional Mix Designs and Alternative Optimization Methods

A critical aspect of evaluating concrete mixtures optimized with Scheffe's Simplex Lattice Model involves comparing the results with traditional mix designs and alternative optimization methods. This comparative analysis aims to discern the advantages and limitations of Scheffe's model in achieving superior outcomes [36]. Traditional mix designs, often relying on empirical rules or trial-and-error approaches, serve as benchmarks for assessing the efficiency and precision brought about by statistical optimization [36]. Furthermore, alternative optimization methods, such as response surface methodologies or genetic algorithms, provide a basis for evaluating the unique contributions of Scheffe's model to the field of concrete mixture design. This comparative analysis informs researchers and practitioners about the relative merits and contexts in which Scheffe's Simplex Lattice Model excels [37]. Table 5 provides a concise overview of the comparative analysis of concrete mixtures optimized

Table 5. Comparison of concrete mixtures optimized with Scheffe's Simplex Lattice Model, traditional mix designs, and alternative optimization methods

Comparison aspect	Description	Reference
Optimization approach	Comparison between Scheffe's Simplex Lattice Model, traditional mix designs (empirical or trial-and-error), and alternative methods like response surface methodologies or genetic algorithms.	[36]
Efficiency and precision	Assessment of the efficiency and precision achieved by Scheffe's model in comparison to traditional methods, serving as benchmarks.	[36]
Unique contributions	Examination of the unique contributions of Scheffe's model compared to alternative optimization methods, highlighting its specific advantages in concrete mixture design.	[37]
Merits and limitations	Discussion of the relative merits and limitations of Scheffe's Simplex Lattice Model in achieving superior outcomes, informing researchers and practitioners about its contexts of excellence.	[37]

Table 6. Challenges, limitations, and areas for improvement in applying Scheffe's Simplex Lattice Model to concrete mixtures

Discussion aspect	Description	Reference
Complexity of concrete mixture	Challenges arising from the complexity of concrete mixtures involving numerous interacting variables. Model efficacy may be compromised in highly nonlinear relationships or regions where assumptions are not well met.	[37, 38]
Computational demands	Computational challenges, especially in large-scale mixtures or dealing with numerous variables simultaneously. Addressing these demands is crucial for practical applicability.	[39, 40]
Optimization challenges	Potential issues with mathematical optimization when dealing with real-world constraints. Practical constraints in construction scenarios, such as material availability and batching limitations, might not be adequately considered in the optimization process.	[40, 43]
Refinement for nonlinearity and interactions	Areas for improvement include refining the model to better handle nonlinearity and complex interactions among variables. Incorporating advanced optimization algorithms or complementary techniques could enhance adaptability.	[41]
Streamlining computational demands	Efforts to streamline computational demands, making the model more accessible for practical applications.	[39]
Incorporating probabilistic methods	Suggested refinement involves incorporating probabilistic or uncertainty analysis methods within the model to better capture real-world variability, contributing to a more robust optimization process.	[42]
Accommodating practical constraints	Refining the model to accommodate practical constraints in construction, such as material availability and batching limitations, enhancing its utility in real-world scenarios.	[42] [43]

with Scheffe's Simplex Lattice Model, traditional mix designs, and alternative optimization methods, covering key aspects and their respective references.

CHALLENGES AND LIMITATIONS

Discussion of Challenges and Limitations in Applying Scheffe's Simplex Lattice Model to Concrete Mixtures

While Scheffe's Simplex Lattice Model offers significant advantages in optimizing concrete mixtures, it is not without challenges and limitations. One notable challenge lies in the complexity of the concrete mixture itself, which often involves numerous interacting variables [37, 38]. The model's efficacy may be compromised when dealing with highly nonlinear relationships or when the optimization process encounters regions of the parameter space where the model's assumptions are not well met [39]. Additionally, the computational demands of the model may pose challenges, especially when dealing with large-scale mixtures or when considering a plethora of variables simultaneously [39, 40]. Furthermore, the reliance on mathematical optimization might overlook certain practical

constraints that can influence the feasibility of recommended mixtures in real-world construction scenarios.

Identification of Potential Areas for Improvement and Refinement of the Model

To address the challenges and enhance the applicability of Scheffe's Simplex Lattice Model in concrete mixture optimization, several areas for improvement and refinement can be considered [40]. Firstly, refining the model to better handle nonlinearity and complex interactions among variables could significantly improve its performance. Incorporating more advanced optimization algorithms or combining Scheffe's model with other complementary techniques may also enhance its adaptability to diverse concrete mixtures [41]. Moreover, efforts to streamline the computational demands of the model could make it more accessible for practical applications. Additionally, incorporating probabilistic or uncertainty analysis methods within the model could better capture real-world variability, contributing to a more robust optimization process [42]. Lastly, refining the model to accommodate

Table 7. Emerging trends in statistical modeling for concrete mixture optimization and future research directions for improving Scheffe's Simplex Lattice Model

Aspect	Description	Reference
Integration of machine learning	Emerging trend: Integration of machine learning techniques, such as neural networks and genetic algorithms, to handle complex, non-linear relationships within concrete mixtures. This trend enhances the capability to optimize mixtures effectively.	[44]
Data-driven approaches	Emerging trend: Increased use of data-driven approaches, leveraging large datasets and advanced analytics to gain insights into material behaviors. This trend enhances the effectiveness of optimizing concrete mixtures.	[45]
Probabilistic modeling and uncertainty quantification	Emerging trend: Integration of probabilistic modeling and uncertainty quantification, allowing researchers to account for variability and assess the robustness of optimized mixtures in real-world conditions.	[45]
Enhancing adaptability to large-scale designs	Future direction: Research on enhancing Scheffe's Simplex Lattice Model's adaptability to large-scale and complex mixture designs. This may involve refining algorithms or incorporating parallel computing strategies to handle computational demands.	[45, 46]
Integration of machine learning concepts	Future direction: Exploration of integrating machine learning concepts within Scheffe's model to handle non-linear relationships and expand its applicability.	[46]
Development of hybrid models	Future direction: Research on developing hybrid models that combine Scheffe's Simplex Lattice Model with other advanced optimization techniques. This integration aims to capitalize on strengths, overcome limitations, and achieve more robust results.	[46]
Performance under different conditions	Future direction: Investigation of Scheffe's model performance under various environmental conditions and material sources. This research contributes to its applicability in diverse construction scenarios.	[45, 46]
Addressing practical constraints	Future direction: Research focused on addressing practical constraints and incorporating real-world considerations, such as economic feasibility and construction site constraints, to enhance the model's practical utility.	[45, 46]

practical constraints in construction, such as material availability and batching limitations, would further enhance its utility in real-world scenarios [42, 43]. Table 6 summarizes the challenges, limitations, and areas for improvement in applying Scheffe's Simplex Lattice Model to concrete mixtures, providing key insights and corresponding references.

EMERGING TRENDS AND FUTURE DIRECTIONS

Exploration of Emerging Trends in Statistical Modeling for Concrete Mixture Optimization

The exploration of emerging trends in statistical modeling for concrete mixture optimization reveals a dynamic landscape influenced by advancements in technology, data analytics, and materials science [44]. One prominent trend involves the integration of machine learning techniques to complement traditional statistical models. Machine learning algorithms, such as neural networks and genetic algorithms, demonstrate promise in handling complex, non-linear relationships within concrete mixtures. Another trend is the increased use of data-driven approaches, leveraging large datasets and advanced analytics to gain insights into material behaviors and optimize mixtures more effectively [45]. Furthermore, the integration of probabilistic modeling and uncertainty quantification is gaining traction, allowing researchers to account for variability and assess the robustness of optimized mixtures in real-world conditions.

Suggestions for Future Research Directions and Improvements in Applying Scheffe's Simplex Lattice Model to Optimize Concrete Properties

As we look towards the future, several avenues for research and improvement in applying Scheffe's Simplex Lattice Model to optimize concrete properties emerge [45, 46]. Firstly, exploring ways to enhance the model's adaptability to large-scale and complex mixture designs is crucial. This might involve refining the model's algorithms or incorporating parallel computing strategies to handle the computational demands associated with intricate concrete formulations. Additionally, integrating machine learning concepts within Scheffe's model could open new possibilities for handling non-linear relationships and further expanding its applicability [46].

Furthermore, future research could focus on developing hybrid models that combine Scheffe's Simplex Lattice Model with other advanced optimization techniques. This integration could capitalize on the strengths of different approaches, potentially overcoming limitations and achieving more robust results. Moreover, investigating the model's performance under different environmental conditions and varying material sources can contribute to its applicability in diverse construction scenarios. Addressing practical constraints and incorporating real-world considerations, such as economic feasibility and construction site constraints, remains a critical area for future research to enhance the model's practical utility. Table 7 summarizes emerging trends in statistical modeling for concrete mixture optimization and suggests future research directions

for improving Scheffé's Simplex Lattice Model, providing key insights and corresponding references.

CONCLUSION

Summary of Key Findings from the Literature Review

The literature review on the application of Scheffé's Simplex Lattice Model in cement concrete mixture optimization reveals a robust and versatile statistical tool. The model has been successfully employed to navigate the complex landscape of concrete mixtures, showcasing its efficacy in achieving optimal combinations of variables. Studies reviewed demonstrate the model's ability to improve performance indicators, such as compressive strength and durability, through a systematic exploration of the design space. The review underscores Scheffé's model as a valuable asset in the evolution of concrete mixture design methodologies.

Implications for the Field of Concrete Mixture Design and Optimization

The implications for the field of concrete mixture design and optimization are significant. The systematic and data-driven approach offered by Scheffé's Simplex Lattice Model presents a paradigm shift from traditional empirical methods. By efficiently exploring multi-variable systems, the model contributes to a more nuanced understanding of the relationships among concrete components. This has profound implications for achieving tailored material properties, enhancing durability, and optimizing sustainability in concrete construction. The reviewed studies suggest that the adoption of Scheffé's model can lead to more efficient and precise concrete mixture designs, setting the stage for advancements in the construction industry.

Call to Action for Further Research and Development in this Area

The literature review illuminates avenues for further research and development in the application of Scheffé's Simplex Lattice Model to concrete mixture optimization. Researchers are encouraged to delve deeper into refining the model to address challenges such as non-linearity and computational efficiency. Exploring hybrid models that integrate Scheffé's model with emerging machine learning techniques offers a promising direction. Additionally, there is a call for research that extends the model's applicability to diverse environmental conditions, material sources, and practical constraints encountered in real-world construction settings. This comprehensive approach will contribute to the continued evolution of concrete mixture design methodologies, advancing the field towards more sustainable, resilient, and high-performance concrete materials.

In conclusion, the literature review showcases Scheffé's Simplex Lattice Model as a valuable tool in concrete mixture optimization, with implications for improving material properties and sustainability. The call to action emphasizes the need for ongoing research and development to refine the model, explore emerging trends, and address practical challenges, fostering innovation in the field of concrete mixture design and optimization.

ACKNOWLEDGEMENTS

The completion of this article is a testament to the collective dedication and invaluable contributions of all authors, whose diverse perspectives and expertise greatly enriched its content and depth.

DATA AVAILABILITY STATEMENT

The author confirm that the data that supports the findings of this study are available within the article. Raw data that support the finding of this study are available from the corresponding author, upon reasonable request.

CONFLICT OF INTEREST

The author declared no potential conflicts of interest with respect to the research, authorship, and/or publication of this article.

USE OF AI FOR WRITING ASSISTANCE

Not declared.

ETHICS

There are no ethical issues with the publication of this manuscript.

REFERENCES

- [1] M. Adamson, A. Razmjoo, and A. Poursaei, "Durability of concrete incorporating crushed brick as coarse aggregate," *Construction and Building Materials*, Vol. 94, pp. 426–434, 2015. [\[CrossRef\]](#)
- [2] E. Avci, and E. Yildirim, "Examination of unconfined compressive strength values by response surface models in grouted sands with microfine cements," *ZBORNİK RADOVA GEO-EXPO*, 2018. [\[CrossRef\]](#)
- [3] R. Kazemi, E. M. Golafshani, and A. Behnood, "Compressive strength prediction of sustainable concrete containing waste foundry sand using meta-heuristic optimization-based hybrid artificial neural network," *Structural Concrete*, 2023. [\[CrossRef\]](#)
- [4] M. A. Mosabehpranah and O. Eren, "Statistical flexural toughness modeling of ultra high performance concrete using response surface method," *Computers and Concrete*, Vol. 17(4), pp. 477–488, 2016. [\[CrossRef\]](#)
- [5] V. Muthuraman, R. Ramakrishnan, K. Sundaravadivu, and B. Arun, "Predicting surface roughness of WEDMed Wc-Co composite using box-behnken response surface method," *Advanced Materials Research*, Vol. 651, pp. 361–366, 2013. [\[CrossRef\]](#)
- [6] I. Z. Akobo, S. B. Akpila, and B. Okedeyi, "Optimization of compressive strength of concrete containing rubber chips as coarse aggregate based on Scheffé's model," *International Journal of Civil Engineering*, Vol. 7(7), pp. 93–110, 2020. [\[CrossRef\]](#)
- [7] U. Alaneme George and M. Mbadike Elvis, "Optimization of flexural strength of palm nut fibre concrete using Scheffé's theory," *Materials Science for Energy Technologies*, Vol. 2(2), pp. 272–287, 2019. [\[CrossRef\]](#)

- [8] A. A. Aliabdo, A. M. Abd-Emoatry, and H. H. Hassan, "Utilization of crushed clay brick in concrete industry," *Alexandria Engineering Journal*, Vol. 53(1), pp. 151–168, 2014. [\[CrossRef\]](#)
- [9] A. V. Alves, T. F. Vieira, J. Brito, and J. R. Correia, "Mechanical properties of structural concrete with fine recycled ceramic aggregate," *Construction and Building Materials*, Vol. 64, pp. 103–113, 2014. [\[CrossRef\]](#)
- [10] E. E. Ambrose, D. U. Ekpo, I. M. Umoren, and U. S. Ekwere, "Compressive strength and workability of laterized quarry sand concrete," *Nigerian Journal of Technology*, Vol. 36(3), pp. 605–610, 2018. [\[CrossRef\]](#)
- [11] U. C. Anya, "Models for predicting the structural characteristics of sand-quarry dust blocks," Doctorial Dissertation, University of Nigeria, 2015.
- [12] J. I. Arimanwa, D. O. Onwuka, M. C. Arimanwa, and U. S. Onwuka, "Prediction of the compressive strength of aluminum waste–cement concrete using Scheffe's theory," *Journal of Materials in Civil Engineering*, Vol. 24(2), pp. 177–183, 2012. [\[CrossRef\]](#)
- [13] P. O. Awoyera, J. O. Akinmusuru, and J. M. Ndumbuki, "Green concrete production with ceramic wastes and laterite," *Construction and Building Materials*, Vol. 117, pp. 29–36, 2016. [\[CrossRef\]](#)
- [14] B. Benabed, E. H. Kadri, T. Ngo, and A. Bouvet, "Rheology and strength of concrete made with recycled concrete aggregate as replacement of natural aggregates," *Epitoanyag Journal of Silicate Based and Composite Materials*, Vol. 72(2), pp. 48–58, 2020. [\[CrossRef\]](#)
- [15] L. Bloom, and A. Bentur, "New mix designs for fresh and hardened concrete," *ACI Materials Journal*, Vol. 92(2), pp. 143–150, 1995.
- [16] G. E. P. Box, W. G. Hunter, and J. S. Hunter, "Statistics for experimenters: An introduction to design, data analysis, and model building," John Wiley & Sons, New York, 1978.
- [17] M. Daniyal and S. Ahmad, "Application of waste ceramic tile aggregates in concrete," *International Journal of Innovative Research in Science and Engineering Technology*, Vol. 4(12), pp. 12808–12815, 2015.
- [18] M. A. DeRousseau, J. R. Kasprzyk, and W. V. Srubar, "Computational design optimization of concrete mixture: a review," *Cement and Concrete Research*, Vol. 109, pp. 42–53, 2018. [\[CrossRef\]](#)
- [19] N. R. Draper and F. Pukelsheim, "K-models for mixture experiments," *Journal of Quality Technology*, Vol. 29(4), pp. 420–427, 1997.
- [20] H. Elci, "Utilization of crushed floor and wall tile wastes as aggregate in concrete production," *Journal of Cleaner Production*, Vol. 112, pp. 742–752, 2016. [\[CrossRef\]](#)
- [21] H. N. Ezeh, and O. M. Ibearugbulem, "Statistical optimization of concrete mix proportions using Scheffe's simplex theory," *Journal of Engineering and Applied Sciences*, Vol. 4(1), pp. 1–7, 2009.
- [22] A. Halicka, P. Ogrodnik, and B. Zegardlo, "Using ceramic sanitaryware waste as concrete aggregate," *Construction and Building Materials*, Vol. 48, pp. 295–305, 2013. [\[CrossRef\]](#)
- [23] A. Heidari and D. Tavakoli, "A study of the mechanical properties of ground ceramic powder concrete incorporating nano-SiO₂ particles," *Construction and Building Materials*, Vol. 38, pp. 255–264, 2013. [\[CrossRef\]](#)
- [24] D. M. Kannan, S. H. Aboubakr, A. S. El-Dieb, and M. M. Taha, "High performance concrete incorporating ceramic wastes powder as large partial replacement of Portland cement," *Construction and Building Materials*, Vol. 144, pp. 35–41, 2017. [\[CrossRef\]](#)
- [25] V. M. Malhotra, and P. K. Mehta, "Supplementary cementitious materials," *Cement and Concrete Research*, Vol. 32(9), pp. 1525–1537, 2002. [\[CrossRef\]](#)
- [26] E. M. Mbadike, and N. N. Osadebe, "Application of Scheffe's model in optimization of compressive strength of lateritic concrete," *Journal of Civil Engineering and Construction Technology*, Vol. 4(9), pp. 265–274, 2013.
- [27] C. Medina, M. Frias, and M. I. Rojas, "Microstructure and properties of recycled concrete using ceramic sanitary ware industry waste as coarse aggregate," *Construction and Building Materials*, Vol. 31, pp. 112–118, 2012. [\[CrossRef\]](#)
- [28] N. Mohan, A. Gupta, and S. Singh, "Optimization of mix proportions of mineral aggregates for use in polymer concrete using statistical techniques," *Journal of Materials in Civil Engineering*, Vol. 14(6), pp. 521–526, 2002.
- [29] D. C. Montgomery, "Design and analysis of experiments," John Wiley & Sons, 2017.
- [30] A. M. Neville, "Properties of concrete," 5th ed., Pearson Education, 2011.
- [31] S. O. Obam, "A simplex-centroid design for mixture optimization," *Journal of Quality Technology*, Vol. 30(4), pp. 391–403, 1998.
- [32] F. O. Okafor, and O. Oguaghamba, "Procedures for optimization using Scheffe's model," *Journal of Engineering Science and Application*, Vol. 7(1), pp. 36–46, 2010.
- [33] P. N. Onuamah and N. N. Osadebe, "Development of optimized strength model of lateritic hollow block with 4% mound soil inclusion," *Nigerian Journal of Technology*, Vol. 34(1), pp. 1–11, 2015. [\[CrossRef\]](#)
- [34] N. N. Osadebe, C. C. Mbajorgu, and T. U. Nwakonobi, "An optimization model development for laterized concrete mix proportioning in building constructions," *Nigerian Journal of Technology*, Vol. 26(1), pp. 37–45, 2007.
- [35] F. Pacheco-Torgal and S. Jalali, "Reuse of ceramic wastes in concrete," *Construction and Building Materials*, Vol. 24, pp. 832–838, 2010. [\[CrossRef\]](#)
- [36] H. Scheffe, "Experiments with mixtures," *Journal of the Royal Statistical Society. Series B (Methodological)*, Vol. 20(2), pp. 344–360, 1958. [\[CrossRef\]](#)

- [37] H. G. Shruthi, M. E. Gowtham, T. Samreen, and R. P. Syed, "Reuse of ceramic wastes as aggregate in concrete," *International Research Journal of Engineering and Technology*, Vol. 3(7), pp. 115–119, 2016.
- [38] M. Simon, "Statistical experimental design for performing tests on concrete," *Cement and Concrete Research*, Vol. 33(11), pp. 1841–1847, 2003.
- [39] M. J. Simon, "Concrete mixture optimization using statistical methods: Final Report," *Federal Highway Administration, Infrastructure Research and Development*, Georgetown Pike McLean, VA, USA, 2003.
- [40] M. Simon, and V. M. Malhotra, "Statistical experimental design for optimizing concrete mixtures," *ACI Materials Journal*, Vol. 94(3), pp. 193–202, 1997.
- [41] Z. Tahar, B. Benabed, E. H. Kadri, T. Ngo, and A. Bouvet, "Rheology and strength of concrete made with recycled concrete aggregate as replacement of natural aggregates," *Epitoanyag Journal of Silicate Based and Composite Materials*, Vol. 72(2) pp. 48–58, 2020. [\[CrossRef\]](#)
- [42] W. C. Tang, Y. Lo, and A. Nadeem, "Mechanical and dryness shrinkage properties of structural-graded polystyrene aggregate concrete," *Cement and Concrete Composite*, Vol. 30(5), pp. 403–409, 2008. [\[CrossRef\]](#)
- [43] A. Torkittikul, and A. Chaipanich, "Utilization of ceramic waste as fine aggregate within Portland cement and fly ash concrete," *Cement and Concrete Composite*, Vol. 32, pp. 440–449, 2010. [\[CrossRef\]](#)
- [44] B. Zegardlo, M. Szlag, and P. Ogródnik, "Ultra-high strength concrete made with recycled aggregate from sanitary ceramic wastes – the method of production and the interfacial transition zone," *Construction and Building Materials*, Vol. 122, pp. 736–742, 2016. [\[CrossRef\]](#)
- [45] O. Zimbili, W. Salim, and M. Ndambuki, "A review on the usage of ceramic wastes in concrete production," *International Journal of Civil, Environmental, Structural, Construction and Architectural Engineering*, Vol. 8(1), pp. 91–95, 2014.
- [46] E. E. Ambrose, F. O. Okafor, and M. E. Onyia, "Compressive strength and Scheffé's optimization of mechanical properties of recycled ceramics tile aggregate concrete," *Journal of Silicate Based and Composite Materials*, Vol. 73(3), Article 18583, 2021. [\[CrossRef\]](#)